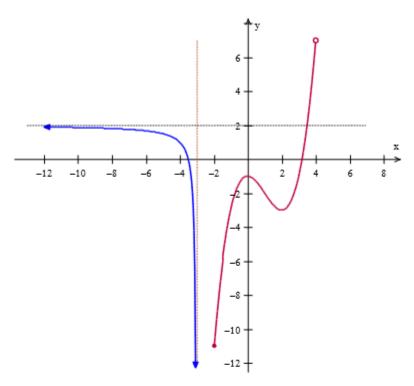
FUNCTIONS, LIMITS AND CONTINUITY - 4th COURSE OF ESO - B

Exercise 1: (2 points) Given the graph of the following function



- a) Study its domain and the image of the function
- b) Determine the points where the function crosses the axes
- c) Study its monotony and local and global extrema
- d) Indicate the equations of the asymptotes

Exercise 2: (1 point) Work out the equation of the straight line that passes through the points A(-3, 2) and B(3, 4)

Exercise 3: (1 point) Calculate the value of the following logarithms

a)
$$\log 0.00001 =$$

b)
$$\log_{7} 1 =$$

c)
$$\log_2 1024 =$$

d)
$$\ln e =$$

Exercise 4: (1.5 points) Find the domain of the functions:

a)
$$f(x) = x^5 - 3x^4 + 7x^3 - 8x + 24$$

b)
$$f(x) = \sqrt{x^2 + 7x + 6}$$

c)
$$f(x) = \frac{\sqrt[3]{x^2 - 1}}{x^2 - 25}$$

d)
$$f(x) = \frac{\sqrt{x^2 - 4}}{x^2 - x - 6}$$

Exercise 5: (1.5 points) Work out the value of these limits

a)
$$\lim_{x \to 3} \frac{x^2 + 2x - 15}{x^3 - 4x^2 - 3x + 18} =$$

b)
$$\lim_{x \to -\infty} \frac{5x^2 + 7x - 9}{x + 3} =$$

c)
$$\lim_{x \to -2} \frac{2x+3}{x^2+4x+4} =$$

d)
$$\lim_{n\to\infty} \left(\sqrt{n^2 + 5} - \sqrt{n^2 - 3n} \right) =$$

Exercise 6: (3 points) Study the continuity of the piecewise function given below and plot its graphic

$$f(x) = \begin{cases} 15 + 3x & x < -2 \\ \left(\frac{1}{3}\right)^x & -2 \le x < 1 \\ x^2 - 4x + 3 & 1 \le x < 4 \\ 3 & 4 < x \le 7 \end{cases}$$

With a different colour or a dotted line, and over the same set of axes, draw the graph of $\left|f(x)\right|$